

Modelling intermetallics Phases – II – Laves, μ and σ phases

Combining the Cluster Expansion and the Compound Energy formalisms

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Outline

Introduction

The Laves phase C15



The μ phase



The σ phase



Conclusion and perspectives

Introduction

- Ordered phase, $\phi : (A, B, \dots)_a (A, B, \dots)_b \dots$

- $G^\phi = G(x) + G(y)$

with $G(x) = \sum_i x_i G_i^\circ + \sum_i \sum_j x_i x_j L_{i,j}^x$

$$G(y) = RT \sum_s a^s \sum_i y_i^s \ln y_i^s + \sum_i \sum_j y_i^s y_j^s G_{i,j}^y$$

$$x_i = \sum_s a^s y_i^s$$

The Laves Phase C15

Crystallography

Prototype	Cu₂Mg		
Space Group	<i>Fd$\bar{3}m$</i>		
Pearson Symbol	<i>cF24</i>		
Wyckhoff Position	<i>8(a)</i>	<i>16(d)</i>	
Point Symmetry of Site	<i>$\bar{4}3m$</i>	<i>$\bar{3}m$</i>	
Co-ordination Number	16	12	
Site Occupation	Mg	Cu	

The Laves Phase C15

Cu-Mg

- Old CEF $(\text{Cu},\text{Mg})_2(\text{Cu},\text{Mg})$

$$G^{\text{C15}} = 3RT \sum_s a^s \sum_i x_i \ln x_i + \sum_i \sum_j y_i' y_j'' G_{i:j}^{\text{C15}} \\ + \sum_i \sum_j \sum_k y_i' y_j'' y_k''' L_{i,j:k}^{\text{C15}} + \sum_i \sum_j \sum_k y_i'' y_j''' y_k' L_{k:i,j}^{\text{C15}}$$

- $G_{\text{Cu:Cu}}^{\text{C15}}$ and $G_{\text{Mg:Mg}}^{\text{C15}}$ fixed
- $G_{\text{Cu:Mg}}^{\text{C15}}$, $L_{\text{Cu,Mg:Mg}}^{\text{C15}}$, and $L_{\text{Cu:Cu,Mg}}^{\text{C15}}$ assessed
- $G_{\text{Mg:Cu}}^{\text{C15}} = - G_{\text{Cu:Mg}}^{\text{C15}} + G_{\text{Cu:Cu}}^{\text{C15}} + G_{\text{Mg:Mg}}^{\text{C15}}$ (WS)
- $L_{\text{Cu,Mg:Cu}}^{\text{C15}} = L_{\text{Cu,Mg:Mg}}^{\text{C15}}$, $L_{\text{Mg:Cu,Mg}}^{\text{C15}} = L_{\text{Cu:Cu,Mg}}^{\text{C15}}$

The Laves Phase C15

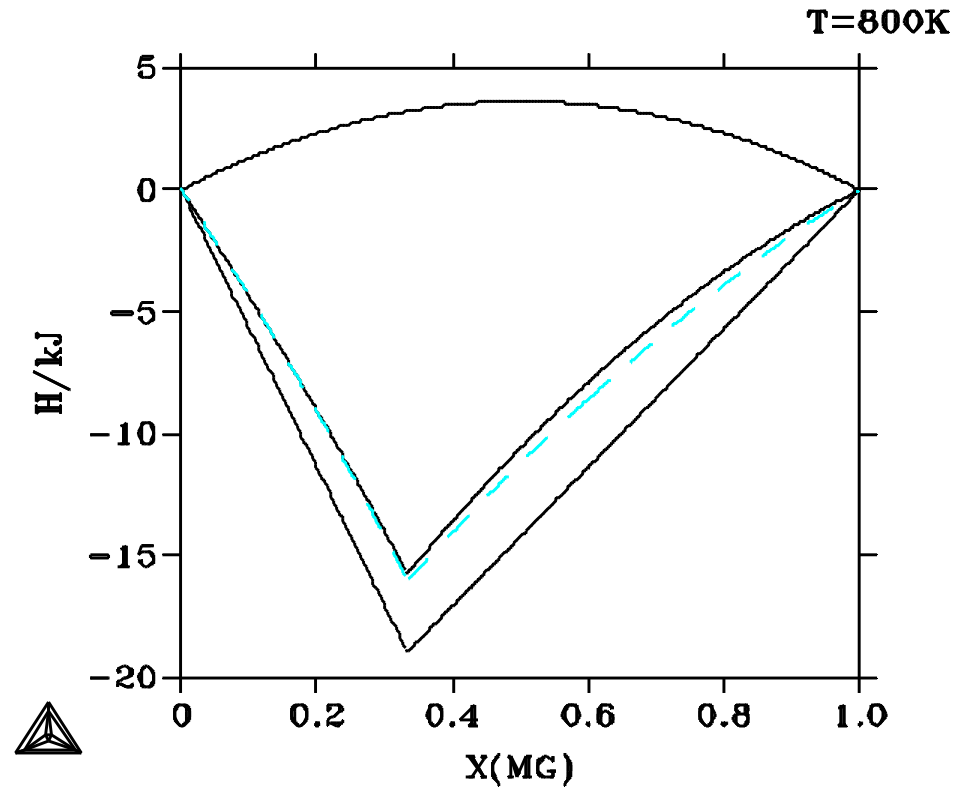
- New modelling (Cu,Mg)₂(Cu,Mg)

$$G^{C15} = \sum_i x_i G_i^\circ + \sum_i \sum_j x_i x_j L_{i,j}^x + RT \sum_s a^s \sum_i y_i^s \ln y_i^s + \sum_i \sum_j y_i^y y_j^y G_{i:j}^y$$

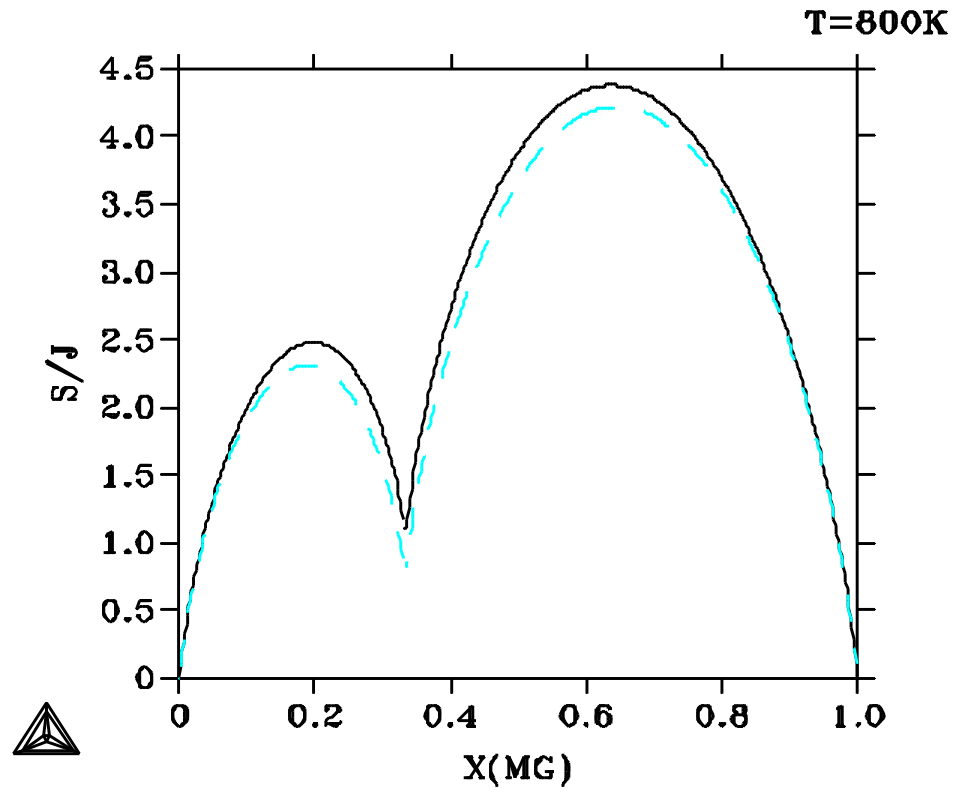
- $G_i^\circ = G_{i:i}^{C15} / 3$, $G_{i:i}^y = 0$ fixed
- $G_{Cu:Mg}^y$ and $L_{Cu,Mg}^x$ assessed
- $G_{Mg:Cu}^y = - G_{Cu:Mg}^y$
- Using initial POP file + C_p

The Laves Phase C15

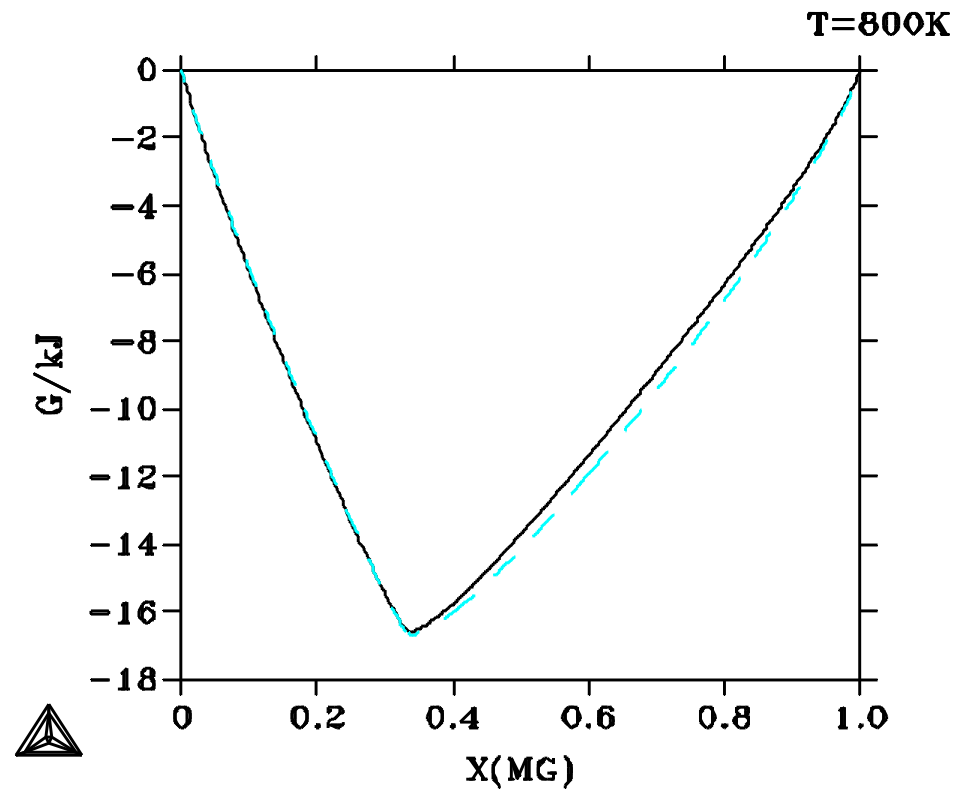
The Laves Phase C15



The Laves Phase C15

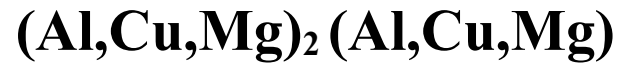


The Laves Phase C15



The Laves Phase C15

- **Al-Cu-Mg**



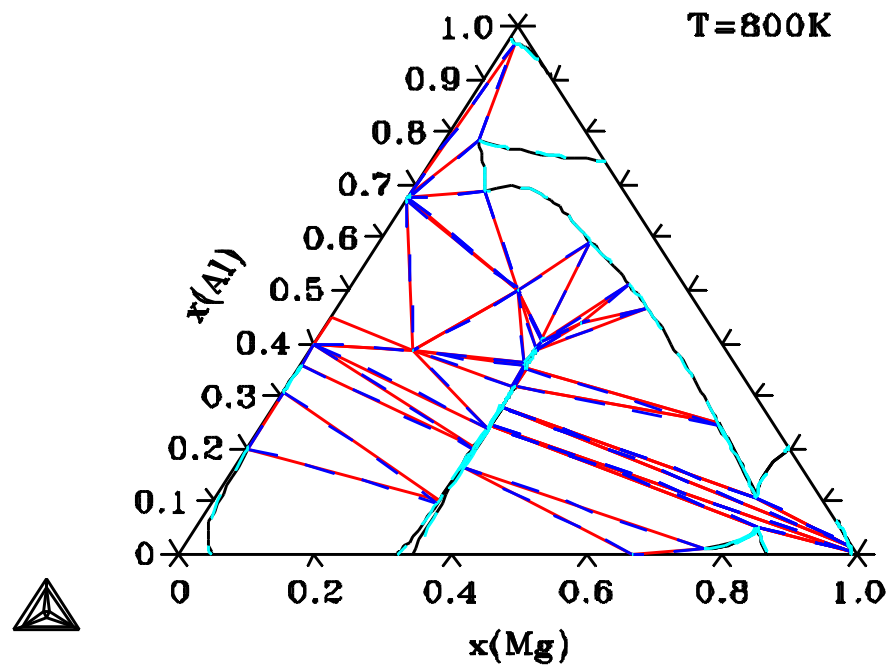
“old” description :

- **many parameters**
- **fixed / assessed parameters ?**

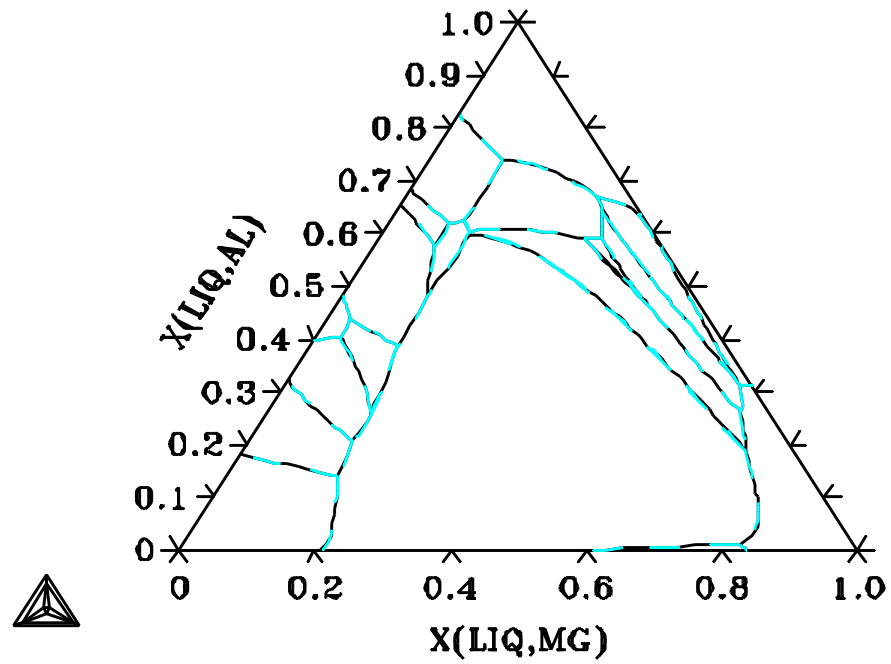
“new” description :

- **POP file had to be modified**
- **less parameters**

The Laves Phase C15



The Laves Phase C15



LAVES_C15

EXCESS MODEL IS REDLICH-KISTER_MUGGIANU

2 SUBLATTICES, SITES 1: 2

CONSTITUENTS: AL,CU,MG : AL,CU,MG

$$G(\text{LAVES_C15,AL:AL;0}) - 3 \text{H298}(\text{FCC_A1,AL;0}) = +15000 + 3 * \text{GHSERAL}$$

$$G(\text{LAVES_C15,CU:AL;0}) - 2 \text{H298}(\text{FCC_A1,AL;0}) - \text{H298}(\text{FCC_A1,CU;0}) = +15000 \\ + 2 * \text{GHSERAL} + \text{GHSERCU}$$

$$G(\text{LAVES_C15,MG:AL;0}) - 2 \text{H298}(\text{FCC_A1,AL;0}) - \text{H298}(\text{HCP_A3,MG;0}) = +\text{C15AL} \\ + 2 * \text{GHSERAL} + \text{GHSERMG}$$

$$G(\text{LAVES_C15,AL:CU;0}) - \text{H298}(\text{FCC_A1,AL;0}) - 2 \text{H298}(\text{FCC_A1,CU;0}) = +15000 \\ + 2 * \text{GHSERCU} + \text{GHSERAL}$$

$$G(\text{LAVES_C15,CU:CU;0}) - 3 \text{H298}(\text{FCC_A1,CU;0}) = +15000 + 3 * \text{GHSERCU}$$

$$G(\text{LAVES_C15,MG:CU;0}) - 2 \text{H298}(\text{FCC_A1,CU;0}) - \text{H298}(\text{HCP_A3,MG;0}) = \\ -54690.99 + 364.73085 * T - 69.276417 * T * \text{LN}(T) - 5.19246\text{E-}04 * T ** 2 \\ + 143502 * T ** (-1) - 5.65953\text{E-}06 * T ** 3$$

$$G(\text{LAVES_C15,AL:MG;0}) - \text{H298}(\text{FCC_A1,AL;0}) - 2 \text{H298}(\text{HCP_A3,MG;0}) = \\ +104970.96 - 16.46448 * T + 2 * \text{GHSERMG} + \text{GHSERCU}$$

$$G(\text{LAVES_C15,CU:MG;0}) - \text{H298}(\text{FCC_A1,CU;0}) - 2 \text{H298}(\text{HCP_A3,MG;0}) = \\ +104970.96 - 16.46448 * T + 2 * \text{GHSERMG} + \text{GHSERCU}$$

$$G(\text{LAVES_C15,MG:MG;0}) - 3 \text{H298}(\text{HCP_A3,MG;0}) = +15000 + 3 * \text{GHSERMG}$$

L(LAVES_C15,AL,MG:AL;0) = +C15MGAL
L(LAVES_C15,AL:AL,CU;0) = +C15ALCU0+C15X
L(LAVES_C15,AL:AL,MG;0) = +C15ALMG0
L(LAVES_C15,CU,MG:AL;0) = +C15MGCU
L(LAVES_C15,CU:AL,CU;0) = +C15ALCU0+C15Y
L(LAVES_C15,CU:AL,MG;0) = +C15ALMG0
L(LAVES_C15,MG:AL,CU;0) = +C15ALCU0
L(LAVES_C15,MG:AL,MG;0) = +C15ALMG0
L(LAVES_C15,AL,MG:CU;0) = +C15MGAL
L(LAVES_C15,AL:CU,MG;0) = +C15CUMG0
L(LAVES_C15,CU,MG:CU;0) = +C15MGCU
L(LAVES_C15,CU:CU,MG;0) = +C15CUMG0
L(LAVES_C15,MG:CU,MG;0) = +C15CUMG0
L(LAVES_C15,AL,MG:MG;0) = +C15MGAL
L(LAVES_C15,CU,MG:MG;0) = +C15MGCU

DIS_C15

\$ THIS PHASE IS THE DISORDERED PART OF LAVES_C15

EXCESS MODEL IS REDLICH-KISTER_MUGGIANU

CONSTITUENTS: AL,CU,MG

$$\mathbf{G(DIS_C15,AL;0)-H298(FCC_A1,AL;0) = +5000+GHSERAL}$$

$$\mathbf{G(DIS_C15,CU;0)-H298(FCC_A1,CU;0) = +5000+GHSERCU}$$

$$\mathbf{G(DIS_C15,MG;0)-H298(HCP_A3,MG;0) = +5000+GHSERMG}$$

$$\mathbf{L(DIS_C15,AL,CU;0) = +V1}$$

$$\mathbf{L(DIS_C15,AL,MG;0) = +V2}$$

$$\mathbf{L(DIS_C15,CU,MG;0) = 14530}$$

LAVES_C15

**\$ THIS PHASE HAS A DISORDERED CONTRIBUTION FROM DIS_C15
EXCESS MODEL IS REDLICH-KISTER_MUGGIANU**

2 SUBLATTICES, SITES 2: 1

CONSTITUENTS: AL,CU,MG : AL,CU,MG

$$\mathbf{G(LAVES_C15,CU:AL;0)-H298(FCC,AL;0)- 2 H298(FCC,CU;0) = +V10}$$

$$\mathbf{G(LAVES_C15,MG:AL;0)-H298(FCC,AL;0)- 2 H298(HCP,MG;0) = -V20-V22*T}$$

$$\mathbf{G(LAVES_C15,AL:CU;0)- 2 H298(FCC,AL;0)-H298(FCC,CU;0) = +V10}$$

$$\mathbf{G(LAVES_C15,MG:CU;0)-H298(FCC,CU;0)- 2 H298(HCP,MG;0) = -C15CUMG}$$

$$\mathbf{G(LAVES_C15,AL:MG;0)- 2 H298(FCC,AL;0)-H298(HCP,MG;0) = +V20+V22*T}$$

$$\mathbf{G(LAVES_C15,CU:MG;0)- 2 H298(FCC,CU;0)-H298(HCP,MG;0) = +C15CUMG}$$

The μ Phase

Crystallography

Prototype	Fe₇W₆				
Space Group	$R\bar{3}m$				
Pearson Symbol	$hR 13$				
Wyckhoff Position	$1(a)$	$2(c)$	$2(c)$	$2(c)$	$6(h)$
Point Symmetry of Site	$\bar{3}m$	$3m$	$3m$	$3m$	m
Co-ordination Number	12	15	16	14	12
Site Occupation	Fe	W	W	W	Fe

The μ Phase

Co-Nb

- Old CEF (Co,Nb) (Co,Nb)₂ (Co)₆ (Nb)₄

$$G^\mu = 13 RT \sum_s a^s \sum_i y_i^s \ln y_i^s + \sum_i \sum_j y_i^i y_j^j G_{i:j:Co:Nb}^\mu$$

- $G_{Co:Co:Co:Nb}^\mu = 7G_{Co}^{fcc} + 2G_{Co}^{bcc} + 4G_{Nb}^{bcc}$

- $G_{Co:Nb:Co:Nb}^\mu = 7G_{Co}^{fcc} + 6G_{Nb}^{bcc} + 13(V1 + V2T)$

- $G_{Nb:Nb:Co:Nb}^\mu = G_{Nb}^{fcc} + 6G_{Co}^{fcc} + 6G_{Nb}^{bcc} + 13(V1 + (V2 + V3)T)$

- $G_{Nb:Co:Co:Nb}^\mu = - G_{Co:Nb:Co:Nb}^\mu + G_{Co:Co:Co:Nb}^\mu + G_{Nb:Nb:Co:Nb}^\mu$
(WS)

The μ Phase

- New modelling (Co,Nb) (Co,Nb)₂ (Co,Nb)₆ (Co,Nb)₄

$$G^\mu = \sum_i x_i G_i^\circ + \sum_i \sum_j x_i x_j L_{i,j}^x + RT \sum_s a^s \sum_i y_i^s \ln y_i^s$$

$$+ \sum_i \sum_j \sum_k \sum_l y_i^j y_j^k y_k^l y_l^i G_{i:j:k:l}^y$$

- $G_i^\circ = (7G_i^{\text{fcc}} + 6G_i^{\text{bcc}})/13$

- $G_{i:j:k:l}^\mu = 0$ except

$$G_{\text{Co:Nb:Co:Nb}}^\mu = V1 + V2T$$

$$G_{\text{Nb:Nb:Co:Nb}}^\mu = V1 + (V2 + V3)T$$

- V1, V2, V3 and $L_{\text{Co,Nb}}^x$ assessed using Kumar's POP file

The μ Phase

MU_PHASE

EXCESS MODEL IS REDLICH-KISTER_MUGGIANU

4 SUBLATTICES, SITES 1: 2: 6: 4

CONSTITUENTS: CO,NB : CO,NB : CO : NB

$$G(\text{MU_PHASE,CO:CO:CO:NB;0}) - 9 \text{H298}(\text{HCP_A3,CO;0}) - 4 \text{H298}(\text{BCC_A2,NB;0}) = + \text{GB}$$

$$G(\text{MU_PHASE,NB:CO:CO:NB;0}) - 8 \text{H298}(\text{HCP_A3,CO;0}) - 5 \text{H298}(\text{BCC_A2,NB;0}) = + \text{GB} + \text{GC} - \text{GA}$$

$$G(\text{MU_PHASE,CO:NB:CO:NB;0}) - 7 \text{H298}(\text{HCP_A3,CO;0}) - 6 \text{H298}(\text{BCC_A2,NB;0}) = + \text{GA}$$

$$G(\text{MU_PHASE,NB:NB:CO:NB;0}) - 6 \text{H298}(\text{HCP_A3,CO;0}) - 7 \text{H298}(\text{BCC_A2,NB;0}) = + \text{GC}$$

$$\text{GA} = +7*\text{GCOFCC}+6*\text{GHSEARNB}+13*(-25810.7251+4.38850*T)$$

$$\text{GB} = +7*\text{GCOFCC}+2*\text{GCOBCC}+4*\text{GHSEARNB}$$

$$\text{GC} = \text{GNBFCC}+6*\text{GHSEARNB}+6*\text{GCOFCC}+13*(-25810.7251+(4.38850-0.52700) *T)$$

DIS_MU

**\$ THIS PHASE IS THE DISORDERED PART OF MU_PHASE
EXCESS MODEL IS REDLICH-KISTER_MUGGIANU
CONSTITUENTS: CO,NB**

$$\begin{aligned}G(\text{DIS_MU,CO;0})-\text{H298}(\text{HCP_A3,CO;0}) &= +\text{GMUA} \\G(\text{DIS_MU,NB;0})-\text{H298}(\text{BCC_A2,NB;0}) &= +\text{GMUB} \\L(\text{DIS_MU,CO,NB;0}) &= 125000\end{aligned}$$

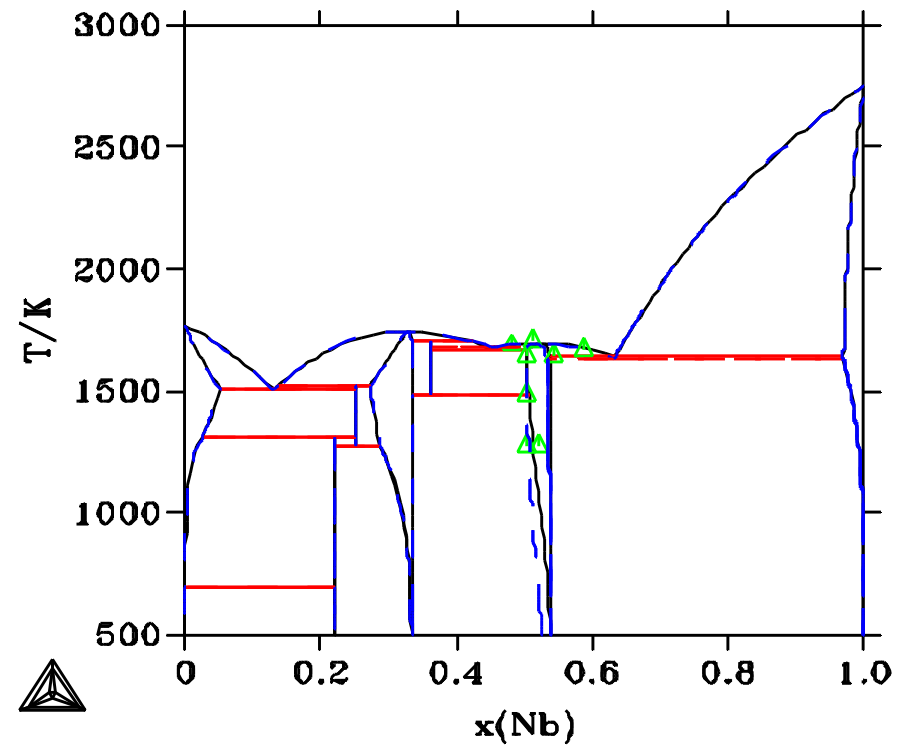
MU_PHASE

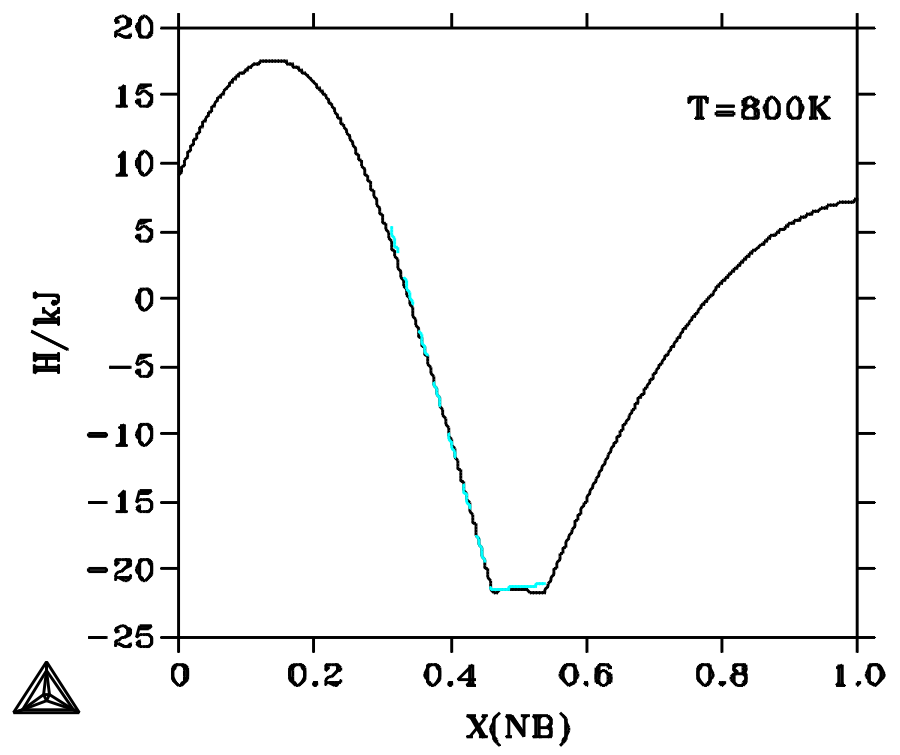
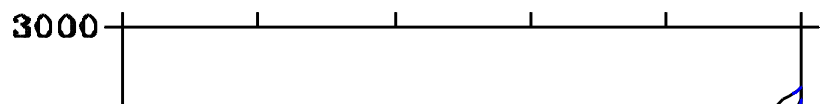
**\$ THIS PHASE HAS A DISORDERED CONTRIBUTION FROM DIS_MU
EXCESS MODEL IS REDLICH-KISTER_MUGGIANU
4 SUBLATTICES, SITES 1: 2: 6: 4
CONSTITUENTS: CO,NB : CO,NB : CO,NB : CO,NB**

$$\begin{aligned}G(\text{MU_PHASE,CO:NB:CO:NB;0})- 7 \text{H298}(\text{HCP,CO;0})- 6 \text{H298}(\text{BCC,NB;0}) &= \\+13*\text{GMUCO7NB} & \\G(\text{MU_PHASE,NB:NB:CO:NB;0})- 6 \text{H298}(\text{HCP,CO;0})- 7 \text{H298}(\text{BCC,NB;0}) &= \\+13*(\text{GMUCO7NB} -0.079*T) &\end{aligned}$$

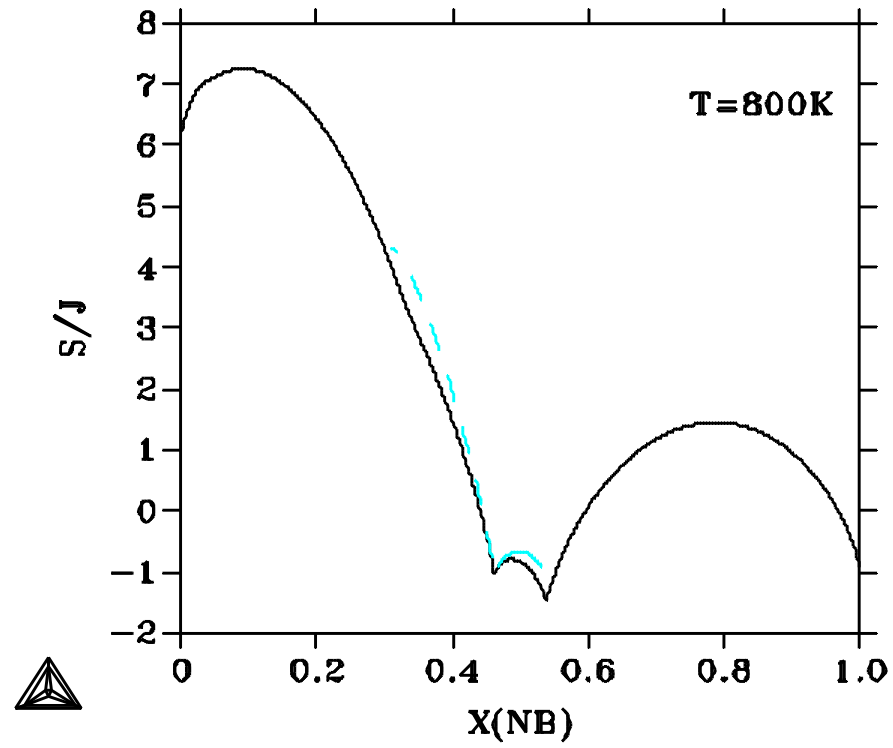
$$\text{GMUCO7NB} = -61000+3.97*T$$

The μ Phase

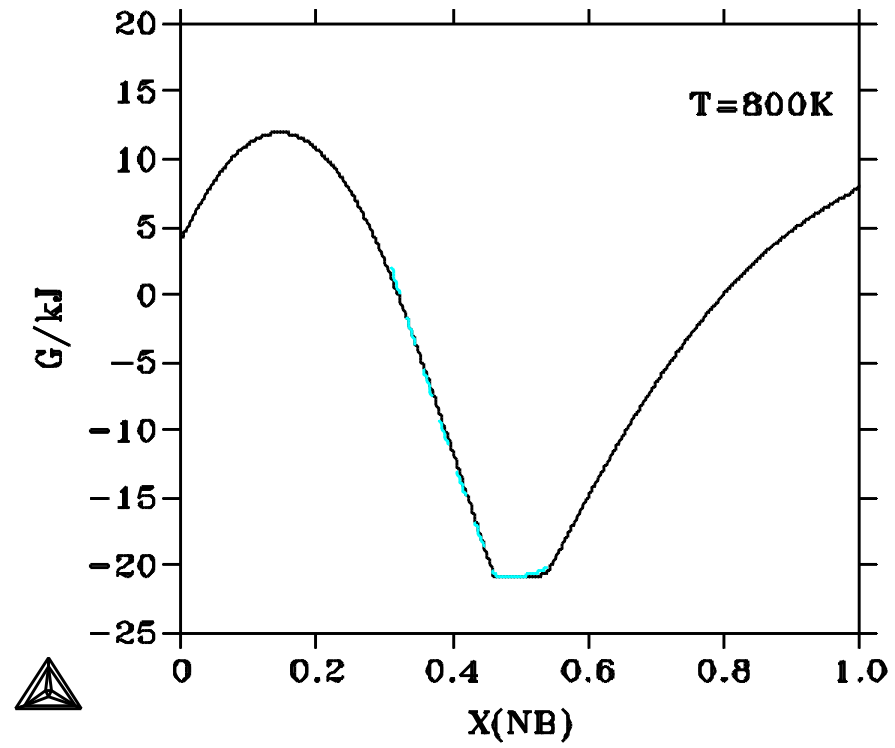




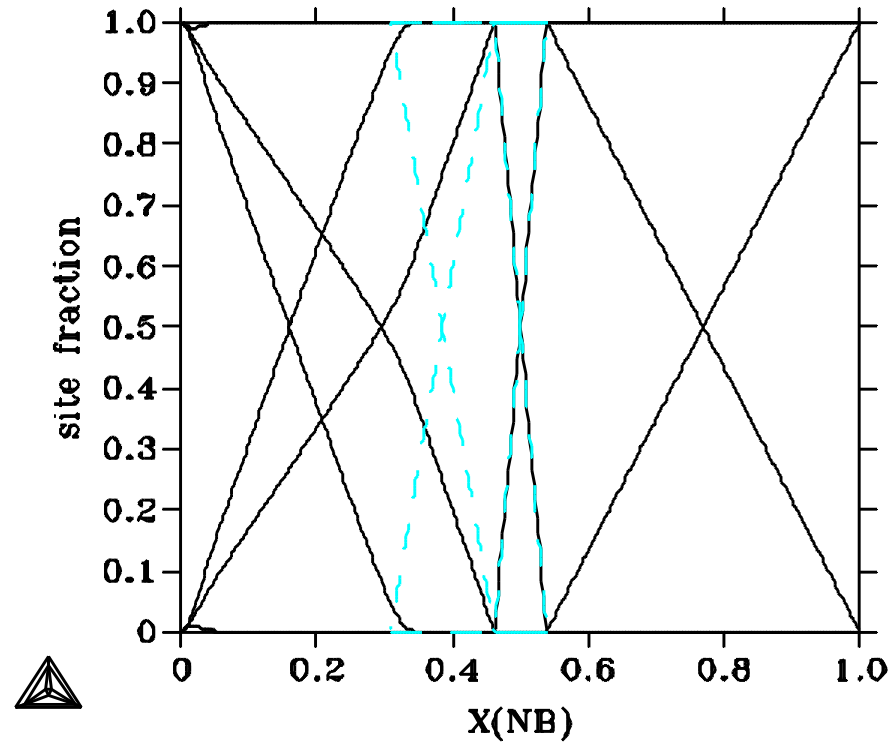
The μ Phase



The μ Phase



The μ Phase



The μ Phase

- New modelling (Co,Nb) (Co,Nb)₂ (Co,Nb)₆ (Co,Nb)₄

$$G^\mu = \sum_i x_i G_i^\circ + \sum_i \sum_j x_i x_j L_{i,j}^x + RT \sum_s a^s \sum_i y_i^s \ln y_i^s$$

$$+ \sum_i \sum_j \sum_k \sum_l y_i^j y_j^k y_k^l y_l^i G_{i:j:k:l}^y$$

- $G_i^\circ = (7G_i^{\text{fcc}} + 6G_i^{\text{bcc}})/13 + 50\,000$

- $G_{i:j:k:l}^\mu = 0$ except

$$G_{\text{Co:Nb:Co:Nb}}^\mu = V1 + V2T$$

$$G_{\text{Nb:Nb:Co:Nb}}^\mu = V1 + (V2 + V3)T$$

- V1, V2, V3 and $L_{\text{Co,Nb}}^x$ assessed using Kumar's POP file

DIS_MU

**\$ THIS PHASE IS THE DISORDERED PART OF MU_PHASE
EXCESS MODEL IS REDLICH-KISTER_MUGGIANU
CONSTITUENTS: CO,NB**

$$\mathbf{G(DIS_MU,CO;0)-H298(HCP_A3,CO;0) = 50000 + GMUA}$$

$$\mathbf{G(DIS_MU,NB;0)-H298(BCC_A2,NB;0) = 50000 + GMUB}$$

$$\mathbf{L(DIS_MU,CO,NB;0) = -140000}$$

MU_PHASE

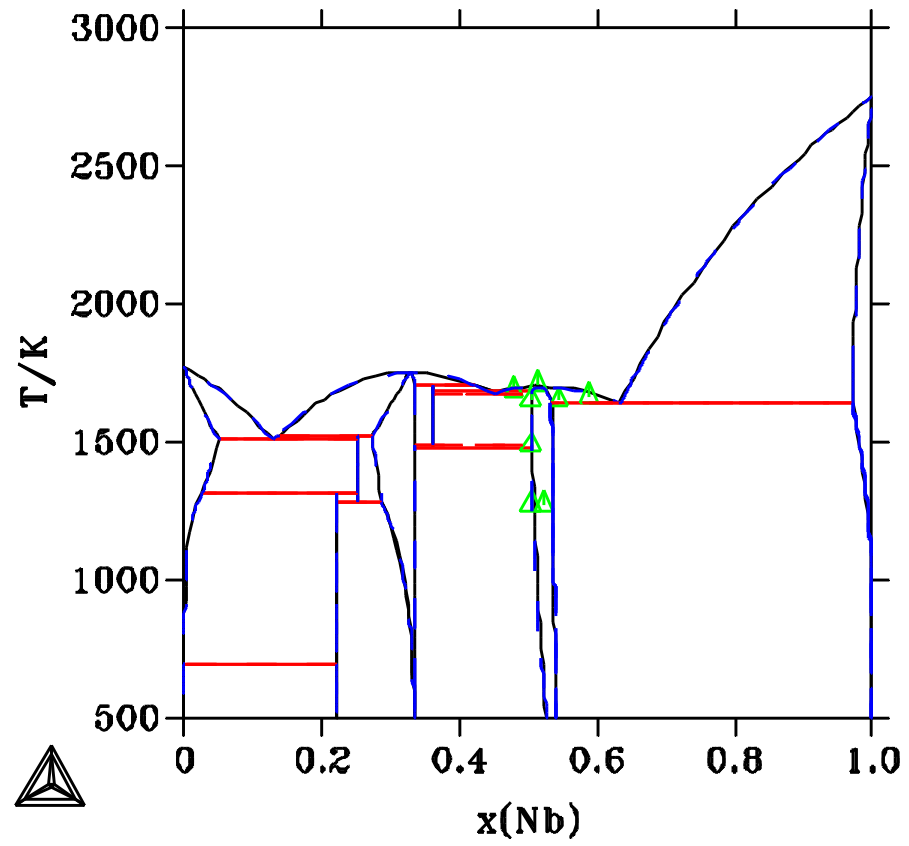
**\$ THIS PHASE HAS A DISORDERED CONTRIBUTION FROM DIS_MU
EXCESS MODEL IS REDLICH-KISTER_MUGGIANU
4 SUBLATTICES, SITES 1: 2: 6: 4
CONSTITUENTS: CO,NB : CO,NB : CO,NB : CO,NB**

$$\mathbf{G(MU_PHASE,CO:NB:CO:NB;0)- 7 H298(HCP,CO;0)- 6 H298(BCC,NB;0) = +13*GMUCO7NB}$$

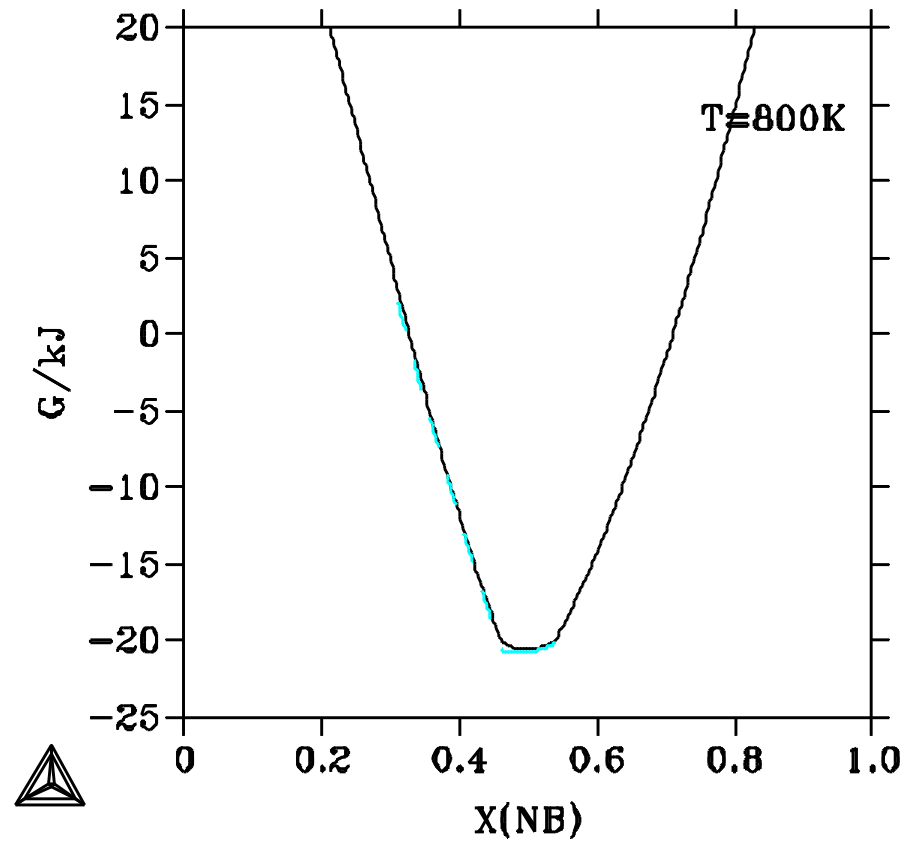
$$\mathbf{G(MU_PHASE,NB:NB:CO:NB;0)- 6 H298(HCP,CO;0)- 7 H298(BCC,NB;0) = +13*(GMUCO7NB -0.22*T)}$$

$$\mathbf{GMUCO7NB = -44200+3.68 *T}$$

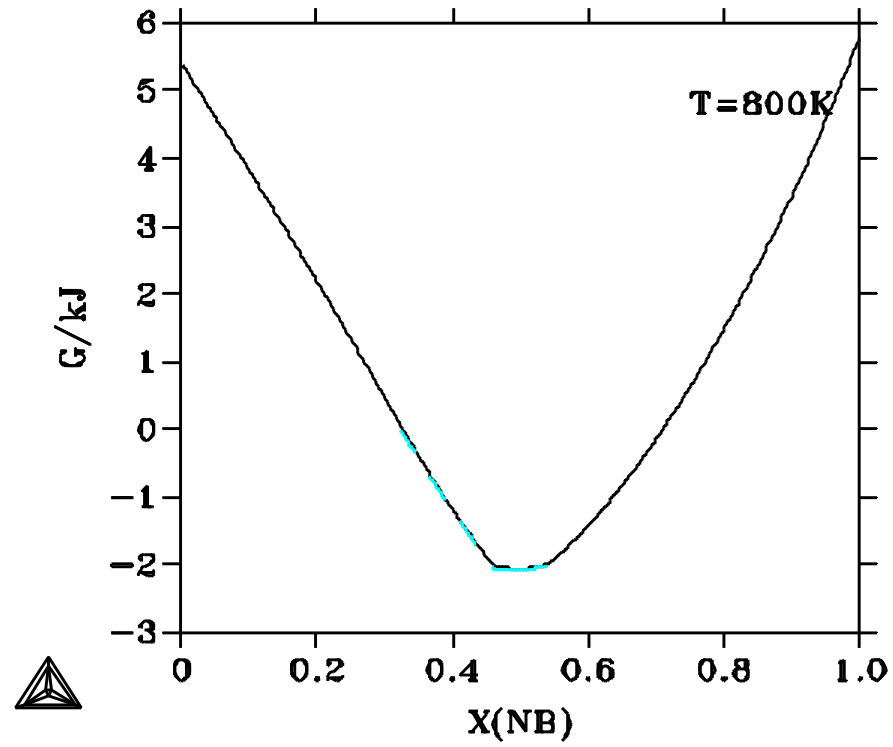
The μ Phase



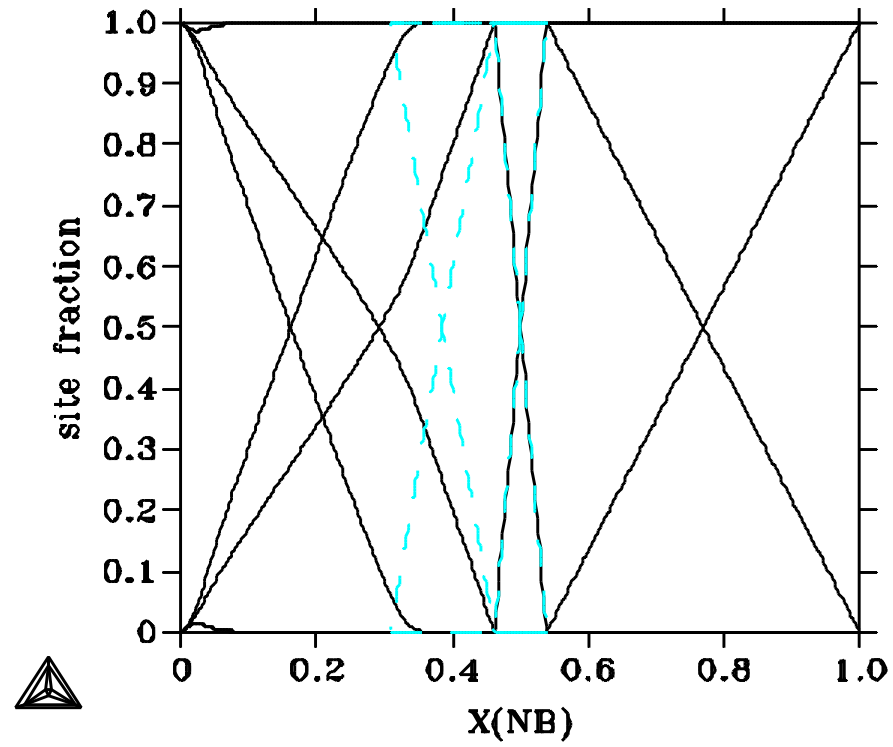
The μ Phase



The μ Phase



The μ Phase



MU_PHASE

**\$ THIS PHASE HAS A DISORDERED CONTRIBUTION FROM DIS_MU
EXCESS MODEL IS REDLICH-KISTER_MUGGIANU**

4 SUBLATTICES, SITES 1: 2: 6: 4

CONSTITUENTS: CO,NB : CO,NB : CO,NB : CO,NB

G(MU_PHASE,CO:CO:CO:CO;0)- 13 H298(HCP,CO;0) = 0.0

G(MU_PHASE,NB:CO:CO:CO;0)- 12 H298(HCP,CO;0)-H298(BCC,NB;0) = 0.0

G(MU_PHASE,CO:NB:CO:CO;0)- 11 H298(HCP,CO;0)- 2 H298(BCC,NB;0) = 0.0

G(MU_PHASE,NB:NB:CO:CO;0)- 10 H298(HCP,CO;0)- 3 H298(BCC,NB;0) = 0.0

G(MU_PHASE,CO:CO:NB:CO;0)- 7 H298(HCP,CO;0)- 6 H298(BCC,NB;0) = 0.0

G(MU_PHASE,NB:CO:NB:CO;0)- 6 H298(HCP,CO;0)- 7 H298(BCC,NB;0) = 0.0

G(MU_PHASE,CO:NB:NB:CO;0)- 5 H298(HCP,CO;0)- 8 H298(BCC,NB;0) = 0.0

G(MU_PHASE,NB:NB:NB:CO;0)- 4 H298(HCP,CO;0)- 9 H298(BCC,NB;0) = 0.0

G(MU_PHASE,CO:CO:CO:NB;0)- 9 H298(HCP,CO;0)- 4 H298(BCC,NB;0) = 0.0

G(MU_PHASE,NB:CO:CO:NB;0)- 8 H298(HCP,CO;0)- 5 H298(BCC,NB;0) = 0.0

G(MU_PHASE,CO:NB:CO:NB;0)- 7 H298(HCP,CO;0)- 6 H298(BCC,NB;0) =

+13*GMUCO7NB

G(MU_PHASE,NB:NB:CO:NB;0)- 6 H298(HCP,CO;0)- 7 H298(BCC,NB;0) =

+13*GMUCO6NB

G(MU_PHASE,CO:CO:NB:NB;0)- 3 H298(HCP,CO;0)- 10 H298(BCC_A2,NB;0) = 0.0

G(MU_PHASE,NB:CO:NB:NB;0)- 2 H298(HCP,CO;0)- 11 H298(BCC_A2,NB;0) = 0.0

G(MU_PHASE,NB:CO:NB:NB;0)- 2 H298(HCP,CO;0)- 11 H298(BCC,NB;0) = 0.0

G(MU_PHASE,CO:NB:NB:NB;0)-H298(HCP,CO;0)- 12 H298(BCC,NB;0) = 0.0

G(MU_PHASE,NB:NB:NB:NB;0)- 13 H298(BCC,NB;0) = 0.0

The σ Phase

Crystallography

Prototype	CrFe				
Space Group	<i>P 4₂/mnm</i>				
Pearson Symbol	<i>tP30</i>				
Wyckhoff Position	<i>2(a)</i>	<i>4(f)</i>	<i>8(i)</i>	<i>8(i)</i>	<i>8(j)</i>
Point Symmetry of Site	<i>mmm</i>	<i>mm</i>	<i>m</i>	<i>m</i>	<i>m</i>
Co-ordination Number	12	15	14	12	14
Site Occupation Fe	88	25	38	84	34

The σ Phase

Cr-Fe

- Old CEF $(\text{Fe})_8 (\text{Cr})_4 (\text{Fe,Cr})_{18}$

$$G^\sigma = 18 RT \sum_i y_i'' \ln y_i'' + \sum_i y_i'' G_{\text{Fe:Cr:i}}^\sigma$$

- $G_{\text{Fe:Cr:Cr}}^\sigma = 8G_{\text{Fe}}^{\text{fcc}} + 22G_{\text{Cr}}^{\text{bcc}} + A + BT$
- $G_{\text{Fe:Cr:Fe}}^\sigma = 8G_{\text{Fe}}^{\text{fcc}} + 4G_{\text{Cr}}^{\text{bcc}} + 18G_{\text{Fe}}^{\text{bcc}} + A' + BT$

The σ Phase

- New modelling $(\text{Fe,Cr})_{10} (\text{Fe,Cr})_4 (\text{Fe,Cr})_{16}$

$$G^\sigma = \sum_i x_i G_i^\circ + \sum_i \sum_j x_i x_j L_{i,j}^x + RT \sum_s a^s \sum_i y_i^s \ln y_i^s$$

$$+ \sum_i \sum_j \sum_k y_i^y y_j^y y_k^y G_{i:j:k}^y$$

- $G_i^\circ = (10G_i^{\text{fcc}} + 20G_i^{\text{bcc}})/30$

- $G_{i:j:k}^y = 0$ except

$$G_{\text{Fe:Cr:Cr}}^y = A + B T$$

$$G_{\text{Fe:Cr:Fe}}^y = A' + B' T$$

- A, A', B, B' and $L_{\text{Cr,Fe}}^x$ assessed using *calculated* POP file

The σ Phase

- New modelling (Fe,Cr)₁₀ (Fe,Cr)₄ (Fe,Cr)₁₆

$$G^{\sigma} = \sum_i x_i G_i^{\circ} + \sum_i \sum_j x_i x_j L_{i,j}^x + RT \sum_s a^s \sum_i y_i^s \ln y_i^s$$

$$+ \sum_i \sum_j \sum_k y_i^y y_j^y y_k^y G_{i:j:k}^y$$

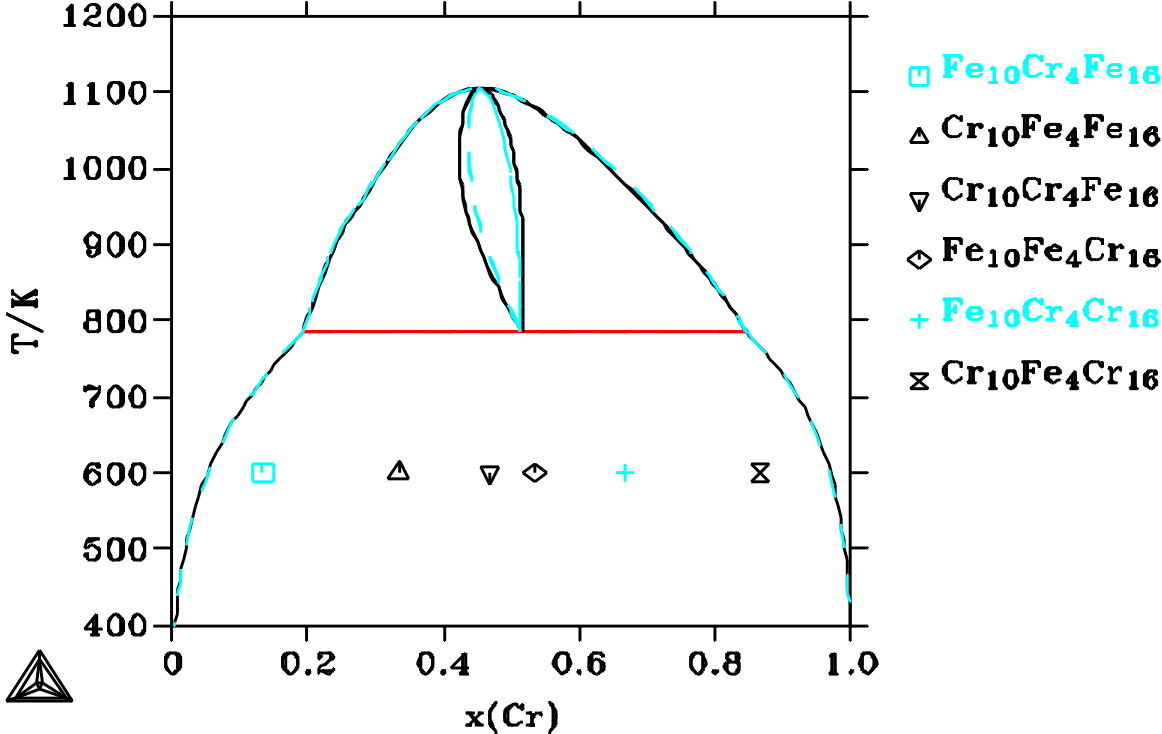
- $G_i^{\circ} = (10G_i^{\text{fcc}} + 20G_i^{\text{bcc}})/30 + 2000$

- $G_{i:j:k}^y = 0$ except

$$G_{\text{Fe:Cr:Cr}}^y \text{ and } G_{\text{Fe:Cr:Fe}}^y$$

- $G_{\text{Fe:Cr:Cr}}^y$, $G_{\text{Fe:Cr:Fe}}^y$ and $L_{\text{Cr,Fe}}^x$ assessed using *calculated* POP file

The σ Phase



The σ Phase

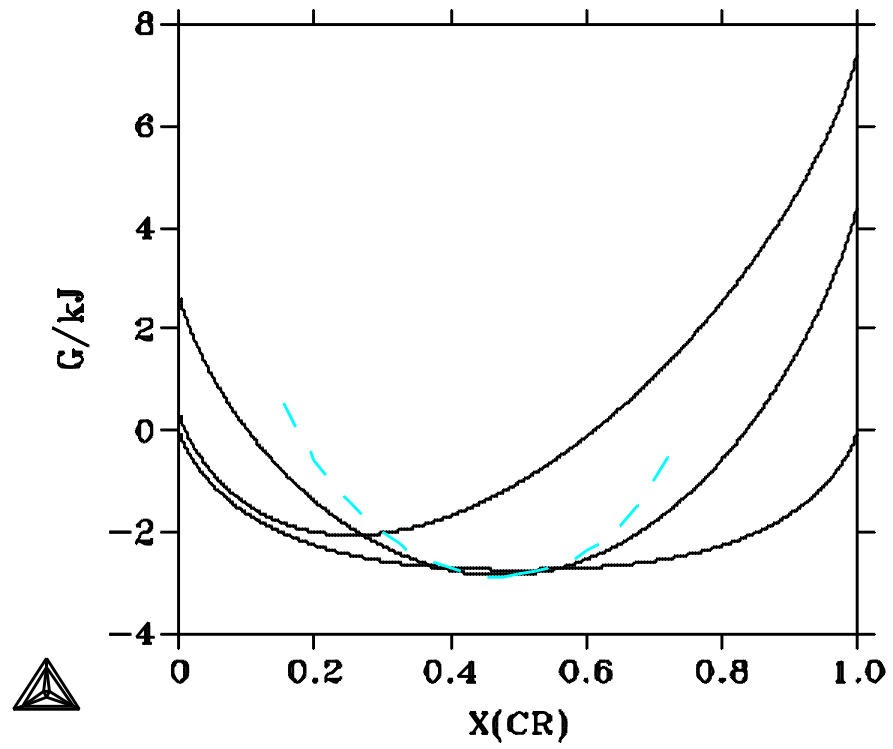
- New modelling (Fe,Cr)₁₀ (Fe,Cr)₄ (Fe,Cr)₁₆

$$G^{\sigma} = \sum_i x_i G_i^{\circ} + \sum_i \sum_j x_i x_j L_{i,j}^x + RT \sum_s a^s \sum_i y_i^s \ln y_i^s$$

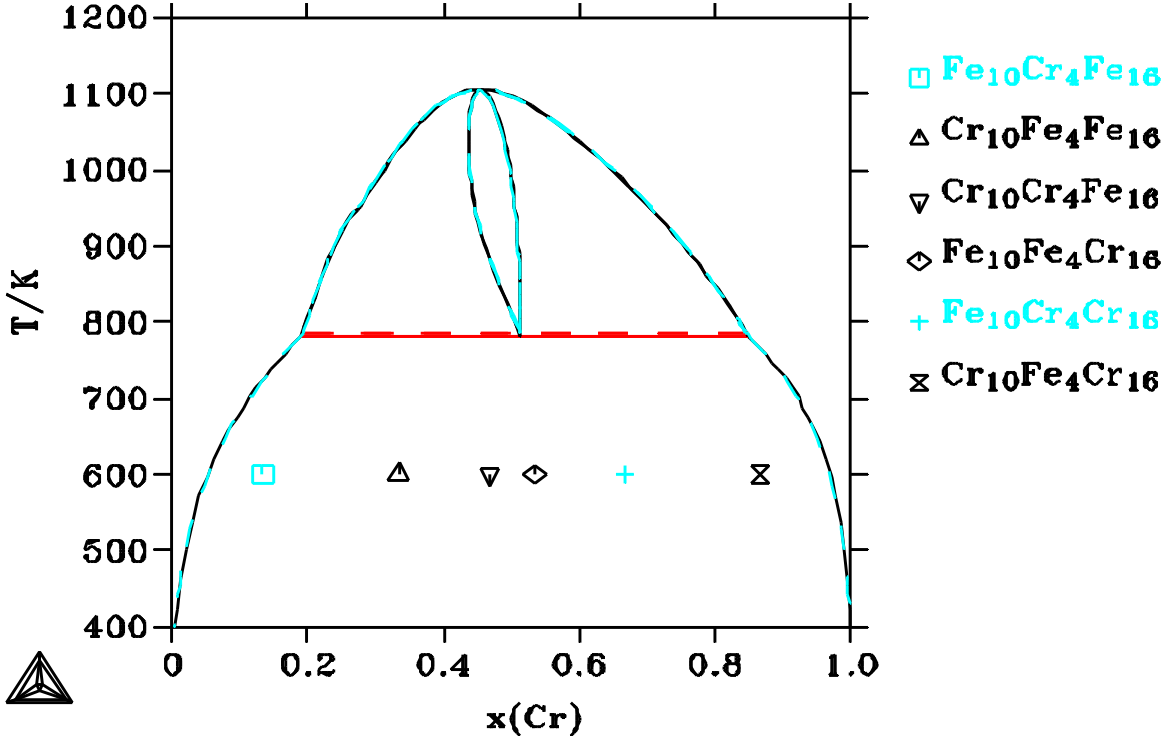
$$+ \sum_i \sum_j \sum_k y_i^j y_j^k y_k^i G_{i:j:k}^y$$

- $L_{Cr,Fe}^x = 0$
- $G_i^{\circ} = (10G_i^{fcc} + 20G_i^{bcc})/30 + V1$
- $G_{i:j:k}^y = 0$ except
 $G_{Fe:Cr:Cr}^y$ and $G_{Fe:Cr:Fe}^y$
- $G_{Fe:Cr:Cr}^y$, $G_{Fe:Cr:Fe}^y$ and V1 assessed using *calculated* POP file

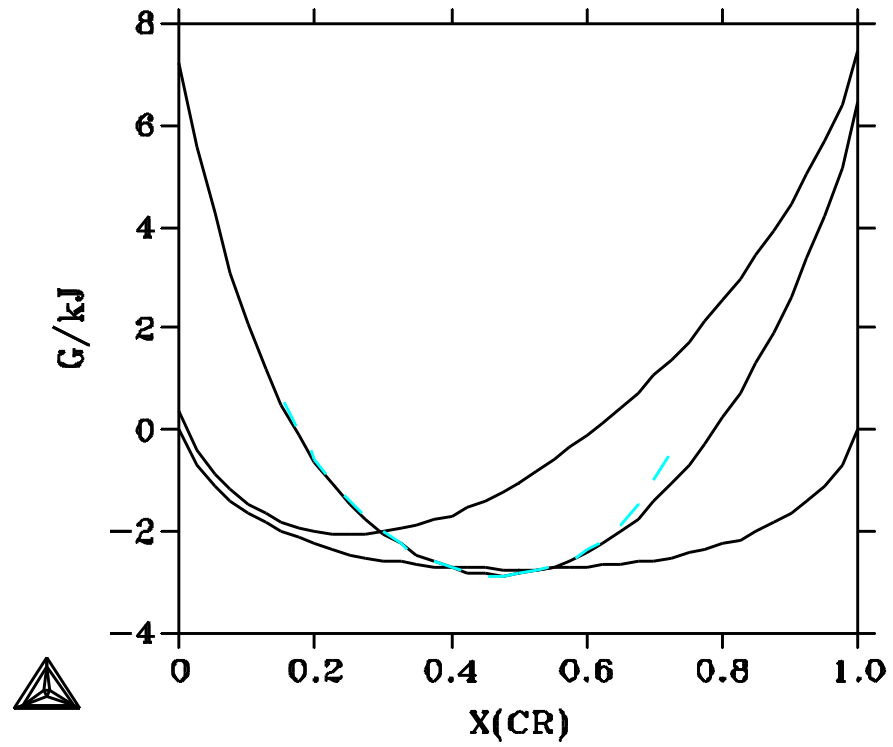
The σ Phase



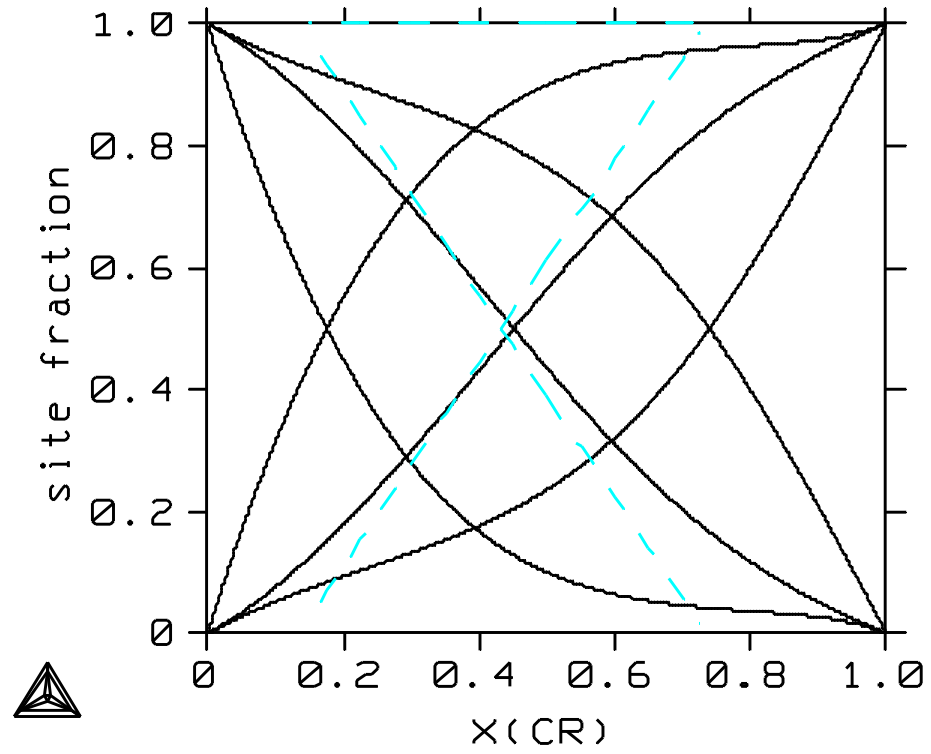
The σ Phase



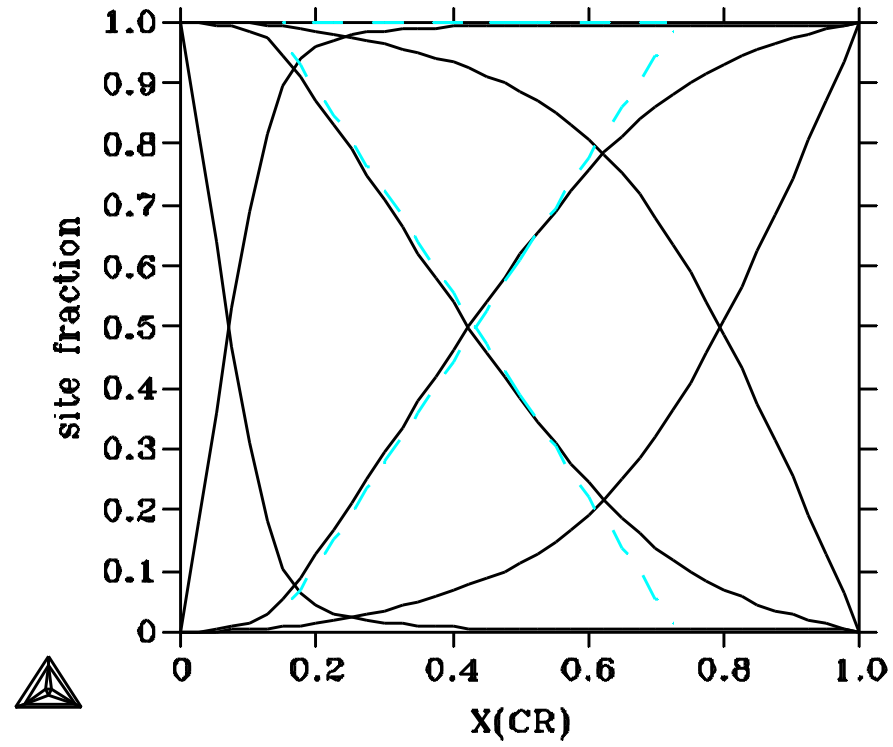
The σ Phase



The σ Phase



The σ Phase



SIGMA

EXCESS MODEL IS REDLICH-KISTER_MUGGIANU

3 SUBLATTICES, SITES 8: 4: 18

CONSTITUENTS: FE,NI : CR : CR,FE,NI

$$G(\text{SIGMA,FE:CR:CR;0}) - 22 H298(\text{BCC_A2,CR;0}) - 8 H298(\text{BCC_A2,FE;0}) = +8*GFEFCC + 22*GHSERCR + 92300 - 95.96*T + GPSIG1$$

$$G(\text{SIGMA,NI:CR:CR;0}) - 22 H298(\text{BCC_A2,CR;0}) - 8 H298(\text{FCC_A1,NI;0}) = +8*GHSERNI + 22*GHSERCR + 221157 - 227*T$$

$$G(\text{SIGMA,FE:CR:FE;0}) - 4 H298(\text{BCC_A2,CR;0}) - 26 H298(\text{BCC_A2,FE;0}) = +8*GFEFCC + 4*GHSERCR + 18*GHSERFE + 117300 - 95.96*T + GPSIG2$$

$$G(\text{SIGMA,NI:CR:FE;0}) - 4 H298(\text{BCC_A2,CR;0}) - 18 H298(\text{BCC_A2,FE;0}) - 8 H298(\text{FCC_A1,NI;0}) = +8*GHSERNI + 4*GHSERCR + 18*GHSERFE$$

$$G(\text{SIGMA,FE:CR:NI;0}) - 4 H298(\text{BCC_A2,CR;0}) - 8 H298(\text{BCC_A2,FE;0}) - 18 H298(\text{FCC_A1,NI;0}) = +8*GFEFCC + 4*GHSERCR + 18*GNIBCC$$

$$G(\text{SIGMA,NI:CR:NI;0}) - 4 H298(\text{BCC_A2,CR;0}) - 26 H298(\text{FCC_A1,NI;0}) = +8*GHSERNI + 4*GHSERCR + 18*GNIBCC + 175400$$

SIGMA

EXCESS MODEL IS REDLICH-KISTER_MUGGIANU

3 SUBLATTICES, SITES 8: 4: 18

CONSTITUENTS: FE,NI : CR : CR,FE,NI

$$\begin{aligned} G(\text{SIGMA,FE:CR:CR;0}) - 22 \text{H298}(\text{BCC_A2,CR;0}) - 8 \text{H298}(\text{BCC_A2,FE;0}) = \\ +8 * \text{GFEFCC} + 22 * \text{GHSERCR} + 92300 - 95.96 * \text{T} + \text{GPSIG1} \end{aligned}$$

$$\begin{aligned} G(\text{SIGMA,NI:CR:CR;0}) - 22 \text{H298}(\text{BCC_A2,CR;0}) - 8 \text{H298}(\text{FCC_A1,NI;0}) = \\ +8 * \text{GHSERNI} + 22 * \text{GHSERCR} \end{aligned}$$

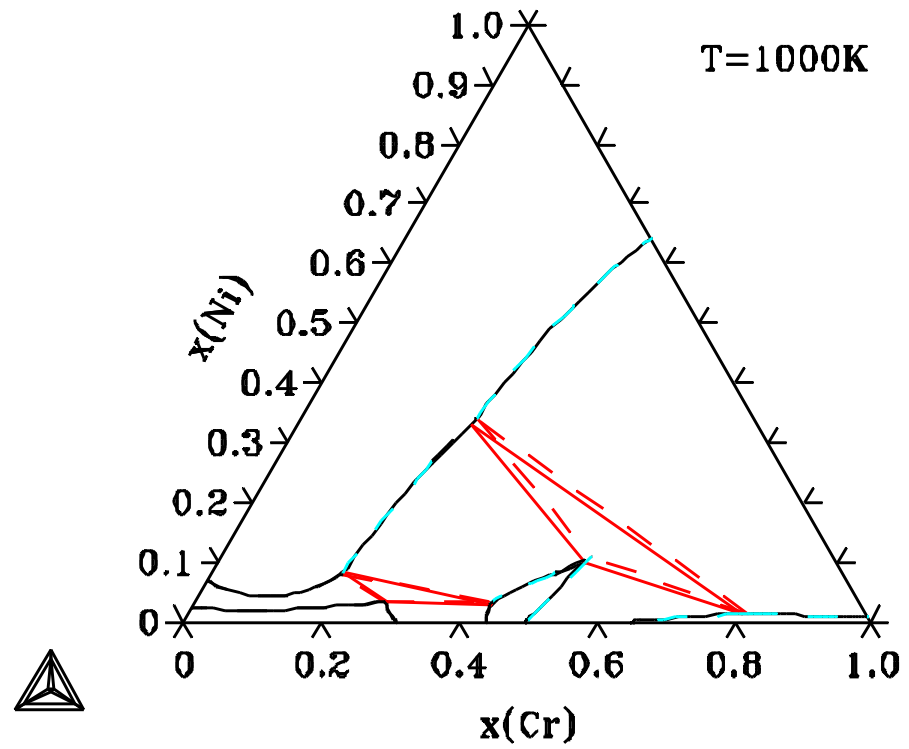
$$\begin{aligned} G(\text{SIGMA,FE:CR:FE;0}) - 4 \text{H298}(\text{BCC_A2,CR;0}) - 26 \text{H298}(\text{BCC_A2,FE;0}) = \\ +8 * \text{GFEFCC} + 4 * \text{GHSERCR} + 18 * \text{GHSERFE} + 117300 - 95.96 * \text{T} + \text{GPSIG2} \end{aligned}$$

$$\begin{aligned} G(\text{SIGMA,NI:CR:FE;0}) - 4 \text{H298}(\text{BCC_A2,CR;0}) - 18 \text{H298}(\text{BCC_A2,FE;0}) - 8 \\ \text{H298}(\text{FCC_A1,NI;0}) = +8 * \text{GHSERNI} + 4 * \text{GHSERCR} + 18 * \text{GHSERFE} \end{aligned}$$

$$\begin{aligned} G(\text{SIGMA,FE:CR:NI;0}) - 4 \text{H298}(\text{BCC_A2,CR;0}) - 8 \text{H298}(\text{BCC_A2,FE;0}) - 18 \\ \text{H298}(\text{FCC_A1,NI;0}) = +8 * \text{GFEFCC} + 4 * \text{GHSERCR} + 18 * \text{GNIBCC} \end{aligned}$$

$$\begin{aligned} G(\text{SIGMA,NI:CR:NI;0}) - 4 \text{H298}(\text{BCC_A2,CR;0}) - 26 \text{H298}(\text{FCC_A1,NI;0}) = \\ +8 * \text{GHSERNI} + 4 * \text{GHSERCR} + 18 * \text{GNIBCC} \end{aligned}$$

The σ Phase



SIGMA

EXCESS MODEL IS REDLICH-KISTER_MUGGIANU

3 SUBLATTICES, SITES 8: 4: 18

CONSTITUENTS: FE,NI : CR : CR,FE,NI

$$\begin{aligned} G(\text{SIGMA,FE:CR:CR;0}) - 22 \text{ H298}(\text{BCC_A2,CR;0}) - 8 \text{ H298}(\text{BCC_A2,FE;0}) = \\ +8 * \text{GFEFCC} + 22 * \text{GHSERCR} + 92300 - 95.96 * \text{T} + \text{GPSIG1} \end{aligned}$$

$$\begin{aligned} G(\text{SIGMA,NI:CR:CR;0}) - 22 \text{ H298}(\text{BCC_A2,CR;0}) - 8 \text{ H298}(\text{FCC_A1,NI;0}) = \\ 0 \end{aligned}$$

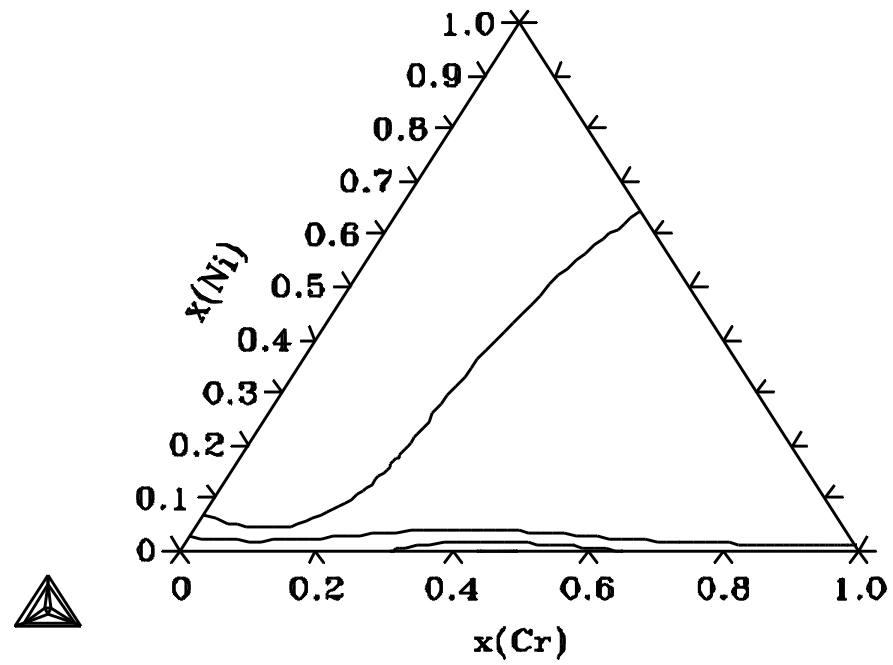
$$\begin{aligned} G(\text{SIGMA,FE:CR:FE;0}) - 4 \text{ H298}(\text{BCC_A2,CR;0}) - 26 \text{ H298}(\text{BCC_A2,FE;0}) = \\ +8 * \text{GFEFCC} + 4 * \text{GHSERCR} + 18 * \text{GHSERFE} + 117300 - 95.96 * \text{T} + \text{GPSIG2} \end{aligned}$$

$$\begin{aligned} G(\text{SIGMA,NI:CR:FE;0}) - 4 \text{ H298}(\text{BCC_A2,CR;0}) - 18 \text{ H298}(\text{BCC_A2,FE;0}) - 8 \\ 0 \end{aligned}$$

$$\begin{aligned} G(\text{SIGMA,FE:CR:NI;0}) - 4 \text{ H298}(\text{BCC_A2,CR;0}) - 8 \text{ H298}(\text{BCC_A2,FE;0}) - 18 \\ \text{H298}(\text{FCC_A1,NI;0}) = 0 \end{aligned}$$

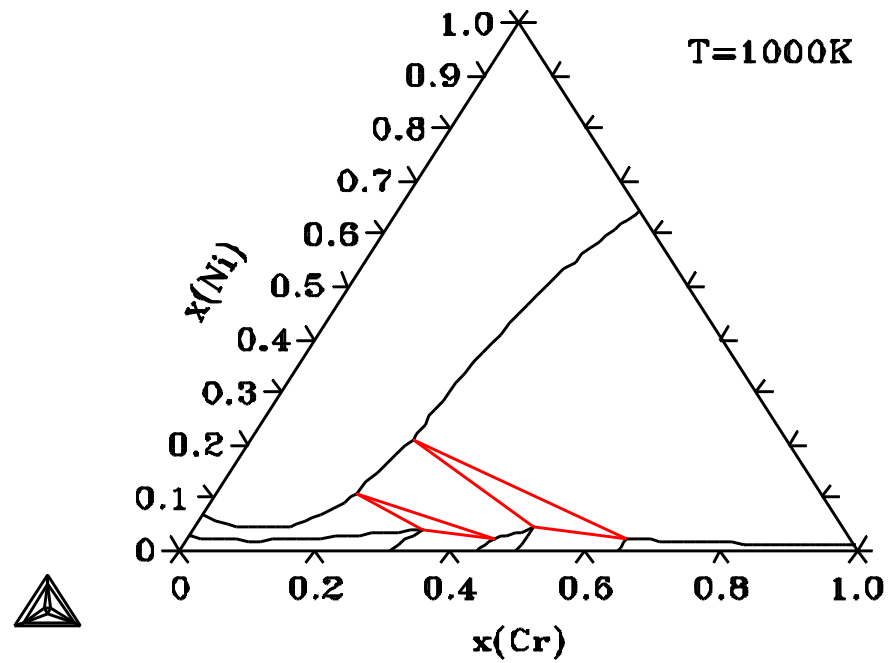
$$\begin{aligned} G(\text{SIGMA,NI:CR:NI;0}) - 4 \text{ H298}(\text{BCC_A2,CR;0}) - 26 \text{ H298}(\text{FCC_A1,NI;0}) = \\ 0 \end{aligned}$$

The σ Phase



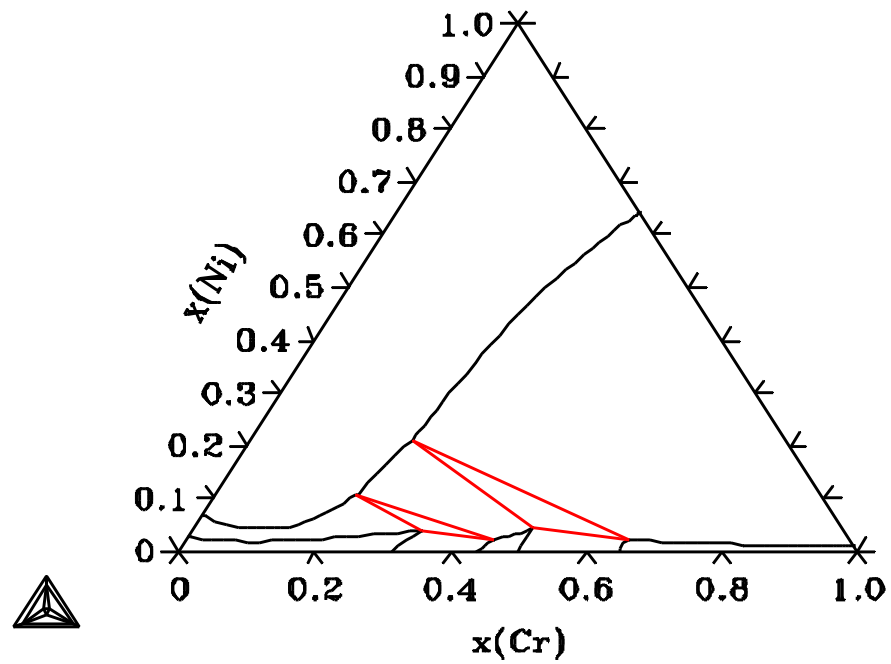
The σ Phase

$$G_{\text{Ni}}^{\circ} = 1000 + G_{\text{Ni}}^{\text{fcc}}$$



The σ Phase

$$G_{\text{Ni}}^{\circ} = 10000 + G_{\text{Ni}}^{\text{fcc}}$$



Conclusions and perspectives

C15 : decrease of the number of parameter

μ and σ phases :

new modelling more physical

not many parameters to be assessed !

need of lattice stability for pure elements

Database for multicomponent systems

less parameters

better extrapolation ?

C14, C15

Conclusions and perspectives

Implemented in ThermoCalc version N